



Recent Advances of Continual Learning

Wei Han





■ Preliminary: Taxonomy of Continual Learning

■ Supervised Continual Learning

■ Unsupervised Continual Learning

■ Our Proposal

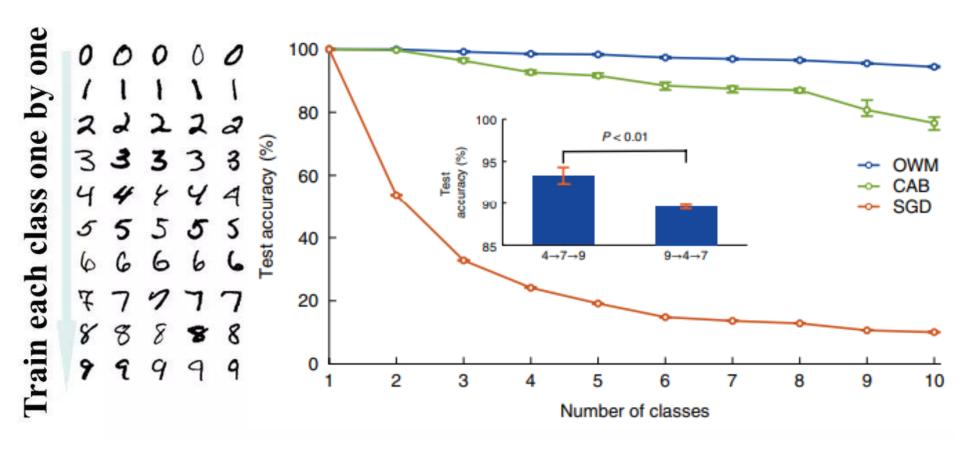


Preliminary:

Taxonomy of Continual Learning

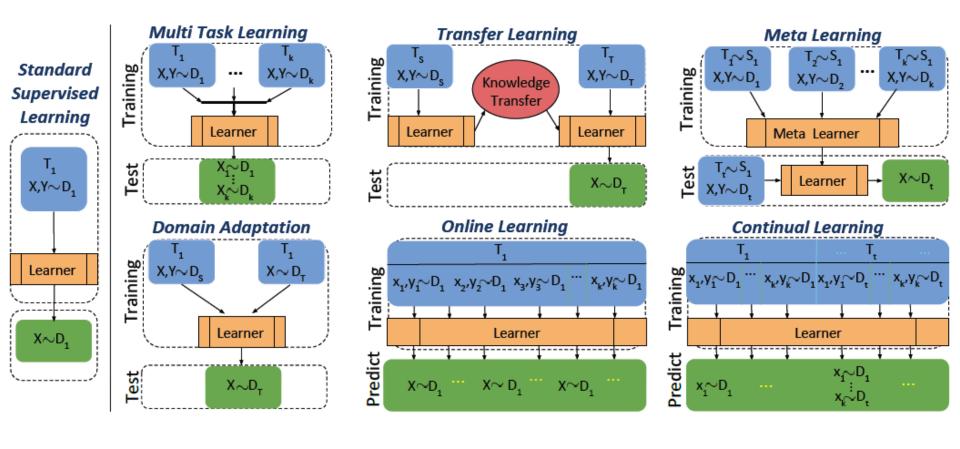


■ Continual Learning



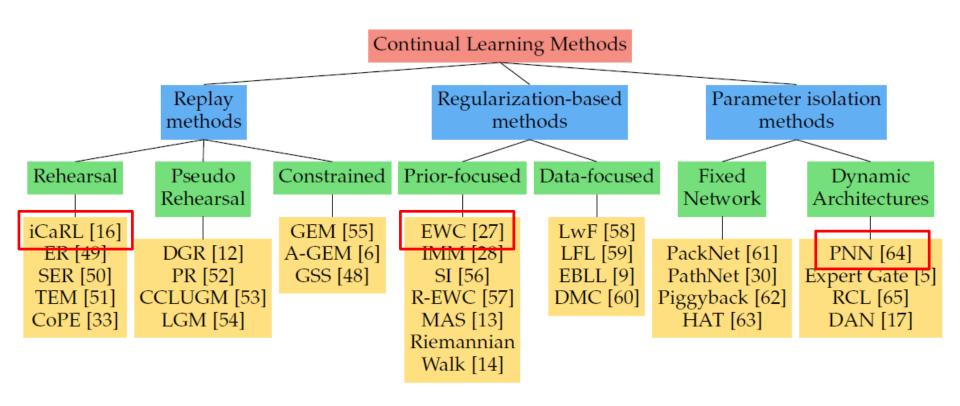


■ Continual Learning





■ Taxonomy of Continual Learning



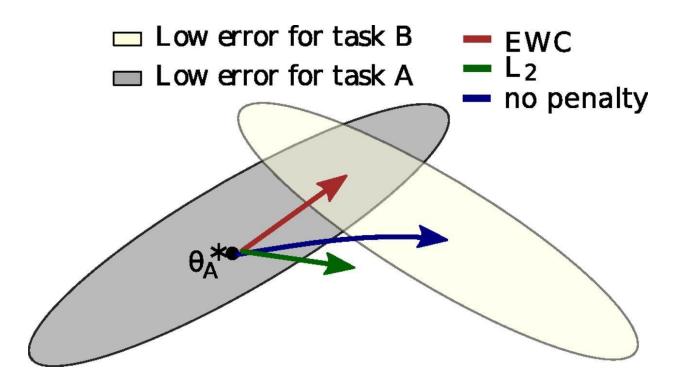


■ iCaRL (Replay-based)

```
Algorithm 2 iCaRL INCREMENTALTRAIN
input X^s, \ldots, X^t // training examples in per-class sets
input K
           // memory size
require (a) // current model parameters
require \mathcal{P} = (P_1, \dots, P_{s-1}) // current exemplar sets
  \Theta \leftarrow \overline{\text{UPDATEREPRESENTATION}}(X^s, \dots, X^t; \mathcal{P}, \Theta)
  m \leftarrow K/t // number of exemplars per class
  for y = 1, ..., s - 1 do
     P_u \leftarrow \text{REDUCEEXEMPLARSET}(P_y, m)
  end for
  for y = s, \dots, t do
     P_y \leftarrow \text{ConstructExemplarSet}(X_y, m, \Theta)
  end for
  \mathcal{P} \leftarrow (P_1, \dots, P_t) // new exemplar sets
```

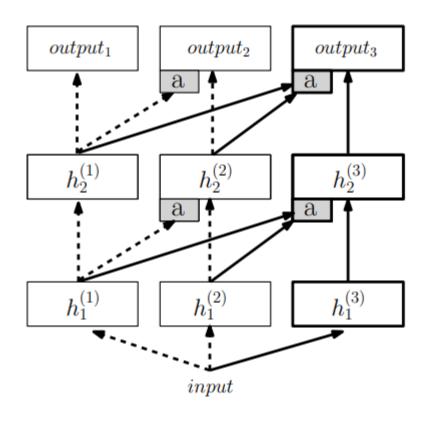


■ EWC (Regularization-based)



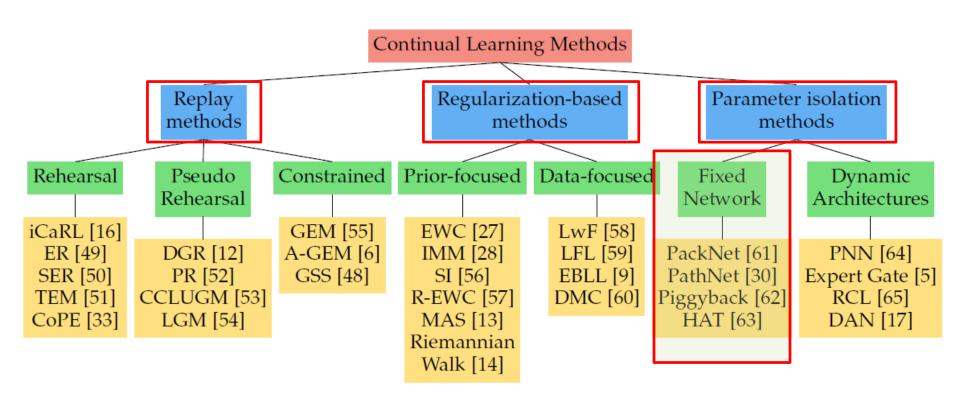


■ PNN (Parameter Isolation)



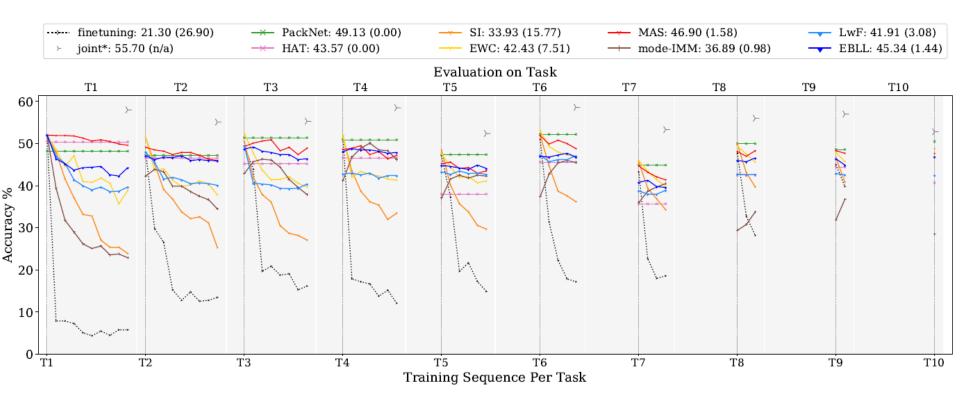


■ Taxonomy of Continual Learning



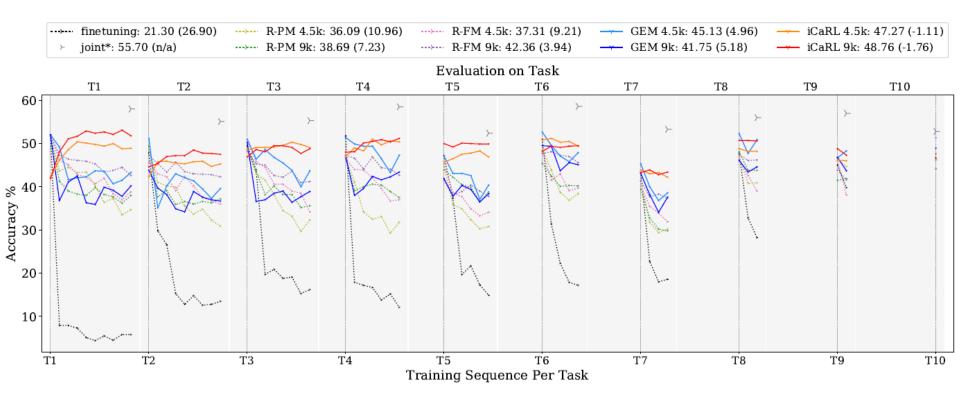


■ Results of Continual Learning





■ Results of Continual Learning

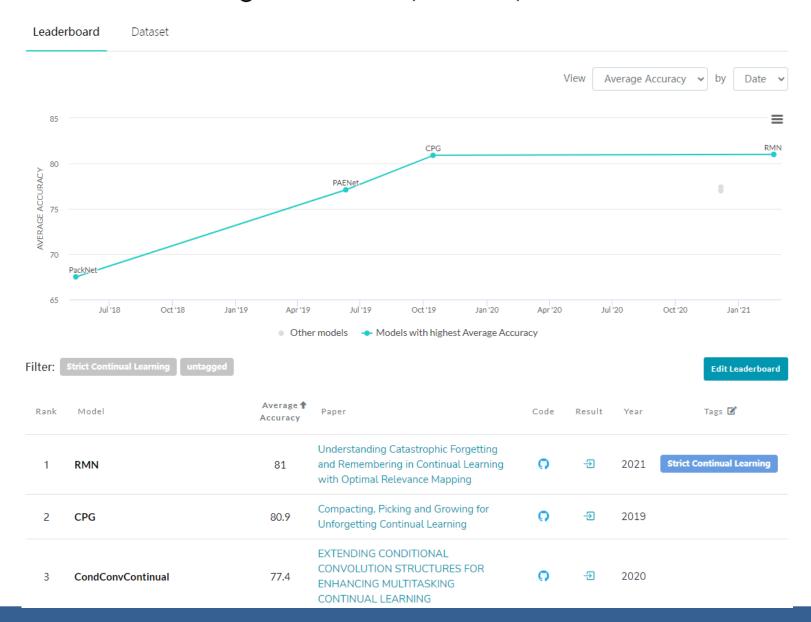




数据挖掘实验室

Data Mining Lab

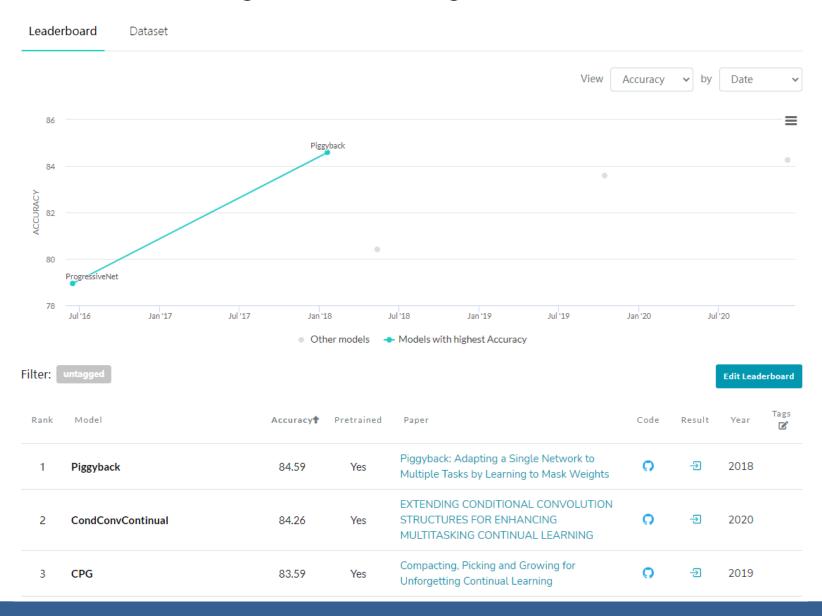
Continual Learning on Cifar 100 (20 tasks)





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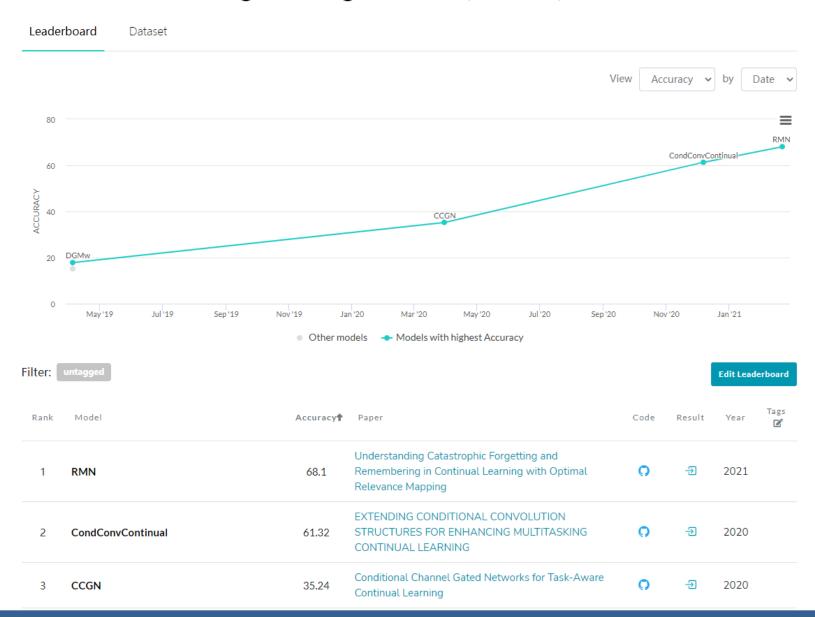
Continual Learning on CUBS (Fine-grained 6 Tasks)





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Continual Learning on ImageNet-50 (5 tasks)



Preliminary

Oxford 102 Flowers					
Method	Task 1	Task 2	Task 3	Task 4	Avg.
Finetuning	10.0 (-20.3)	5.1 (-17.1)	6.7 (-13.6)	17.3 (0.0)	9.8
Freezing	30.3 (0.0)	39.8 (0.0)	32.0 (0.0)	33.1 (0.0)	33.8
Joint	54.6 (+24.3)	58.9 (+11.5)	57.7 (+4.5)	47.0 (0.0)	54.6
EWC [14]	12.1 (-18.2)	11.6 (-38.1)	9.3 (-24.4)	25.8 (0.0)	14.7
HAT [41]	17.2 (-12.7)	19.3 (-28.5)	28.6 (+1.4)	31.6 (0.0)	24.2
PackNet [26]	32.0 (0.0)	53.7 (0.0)	43.6 (0.0)	37.9 (0.0)	41.8
TFM w/o FN	36.4 (0.0)	54.1 (0.0)	38.6 (0.0)	39.0 (0.0)	42.0
TFM	36.4 (0.0)	53.8 (0.0)	45.5 (0.0)	37.6 (0.0)	43.3
CUBS 200 Birds					
Method	Task 1	Task 2	Task 3	Task 4	Avg.
Finetuning	7.4 (-30.2)	2.6 (-30.0)	29.7 (-3.4)	43.1 (0.0)	20.7
Freezing	37.6 (0.0)	35.1 (0.0)	35.4 (0.0)	38.4 (0.0)	36.6
Joint	48.7 (+11.1)	52.1 (+6.0)	50.7 (+1.5)	51.9 (0.0)	50.8
EWC [14]	16.2 (-21.4)	19.0 (-21.2)	24.2 (-14.0)	41.7 (0.0)	25.3
HAT [41]	18.7 (-1.8)	19.4 (-0.4)	28.5 (-0.6)	31.2 (0.0)	24.4
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TFM w/o FN	42.9 (0.0)	44.1 (0.0)	48.3 (0.0)	49.1 (0.0)	46.1
TFM	42.9 (0.0)	43.1 (0.0)	49.9 (0.0)	48.8 (0.0)	46.2
Stanford 40 Actions					
Method	Task 1	Task 2	Task 3	Task 4	Avg.
Finetuning	24.4 (-10.5)	26.5 (-7.7)	17.6 (-16.8)	28.9 (0.0)	24.4
Freezing	34.9 (0.0)	29.4 (0.0)	30.1 (0.0)	30.5 (0.0)	31.2
Joint	45.7 (+10.8)	40.3 (+4.8)	43.2 (-1.1)	40.2 (0.0)	42.4
EWC [14]	24.2 (-10.7)	28.2 (-2.0)	25.2 (-5.6)	34.3 (0.0)	28.0
HAT [41]	25.7 (-1.0)	25.5 (-2.7)	30.1 (-2.1)	34.4 (0.0)	28.9
PackNet [26]	32.5 (0.0)	32.9 (0.0)	36.7 (0.0)	34.3 (0.0)	34.1
TFM w/o FN	35.3 (0.0)	38.3 (0.0)	39.2 (0.0)	38.0 (0.0)	37.7
TFM	35.3 (0.0)	37.2 (0.0)	42.0 (0.0)	37.2 (0.0)	38.0



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Supervised Continual Learning

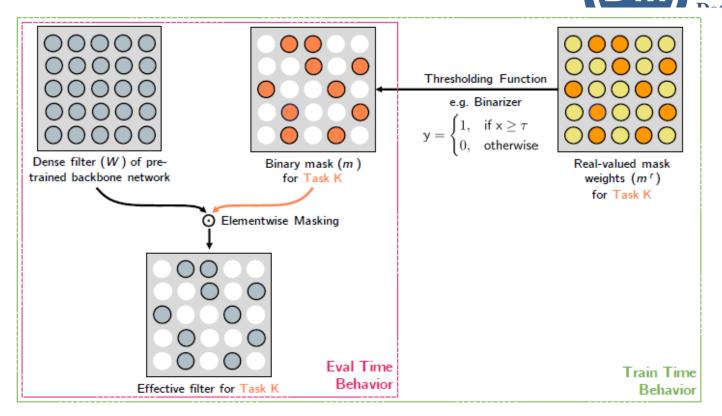
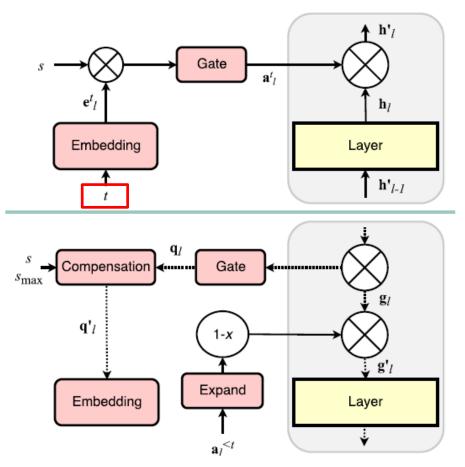


Fig. 1: Overview of our method for learning piggyback masks for fixed backbone networks. During training, we maintain a set of real-valued weights m^r which are passed through a thresholding function to obtain binary-valued masks m. These masks are applied to the weights W of the backbone network in an elementwise fashion, keeping individual weights active, or masked out. The gradients obtained through backpropagation of the task-specific loss are used to update the real-valued mask weights. After training, the real-valued mask weights are discarded and only the thresholded mask is retained, giving one network mask per task.



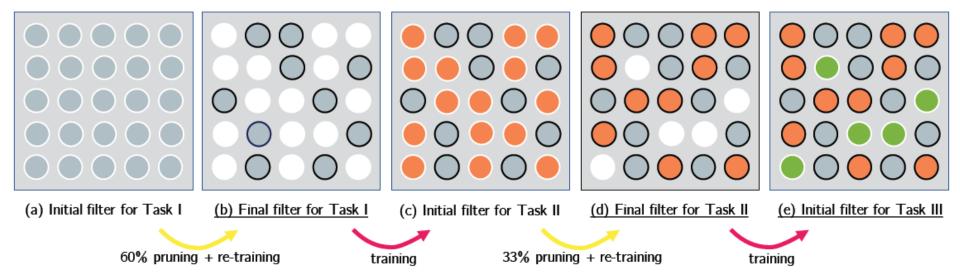
■ Learnable hard attention



$$s = \frac{1}{s_{\text{max}}} + \left(s_{\text{max}} - \frac{1}{s_{\text{max}}}\right) \frac{b-1}{B-1},$$



■ Pruning as Masks



Compacting, Picking and Growing



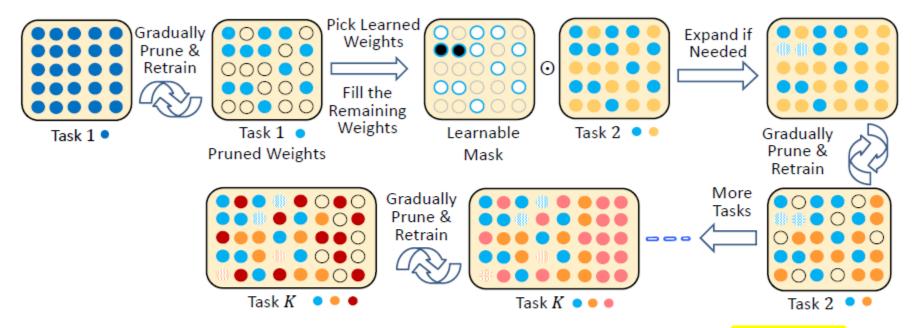


Figure 1: Compacting, Picking, and Growing (CPG) continual learning. Given a well-trained model, gradual pruning is applied to compact the model to release redundant weights. The compact model weights are kept to avoid forgetting. Then a learnable binary weight-picking mask is trained along with previously released space for new tasks to effectively reuse the knowledge of previous tasks. The model can be expanded for new tasks if it does not meet the performance goal. Best viewed in color.

Ternary Feature Map



■ Ternary state: 'used', 'learnable', 'unused'

• Binary mask

$$y = (Wx) \odot m^{t,l}$$

$$\frac{\partial \mathcal{L}}{\partial W_{ij}} = (m_i^{t,l} \wedge m_j^{t,l-1}) x_j \frac{\partial \mathcal{L}}{\partial y_i}$$

Layer N

Layer N+1

Masked: forward / backward





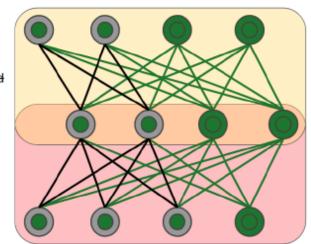
Weights used on T, ,

— Weights used on T₂

Ternary mask — Unused weights
$$y = (Wx) \odot n^{t,l} \qquad n_i^{t,l} = \begin{cases} 1, & \text{if } \exists \ s \leq t \ : m_i^{s,l} = 1 \\ 0, & \text{otherwise} \end{cases}$$

$$\frac{\partial \mathcal{L}}{\partial W_{ij}} = (n_j^{t,l-1} n_i^{t,l} - n_j^{t-1,l-1} n_i^{t-1,l}) x_j \frac{\partial \mathcal{L}}{\partial y_i}$$

$$\frac{\partial \mathcal{L}}{\partial W_{ij}} = (m_i^{t,l} \vee m_j^{t,l-1}) x_j \frac{\partial \mathcal{L}}{\partial y_i}$$





■ Task-specific feature normalization

$$\hat{x}_{l,i} = \gamma_{t,l,i} x_{l,i} + \beta_{t,l,i}$$

Growing Ternary Feature Map

$$n_j^{t,l} = \begin{cases} 1, & \text{for current task, if } 1 \leq j \leq I + N \\ 0, & \text{for previous tasks, if } I < j \leq I + N \end{cases}$$

$$m_j^{t,l} = \begin{cases} 0, & \text{for current task, if } 1 \leq j \leq I \\ 1, & \text{for current task, if } I < j \leq I + N \\ 0, & \text{for previous tasks, if } I < j \leq I + N \end{cases}$$

Summary and Discussion



■ Differentiable Mask?

■ Knowledge Reuse?

■ Expandable?

Computational Complexity (upon weights/features)

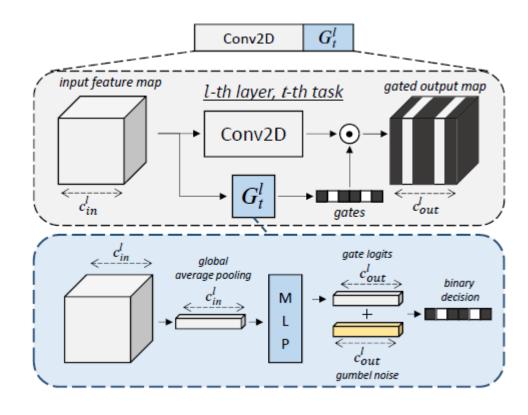


Unsupervised Continual Learning

Conditional Channel Gated Networks



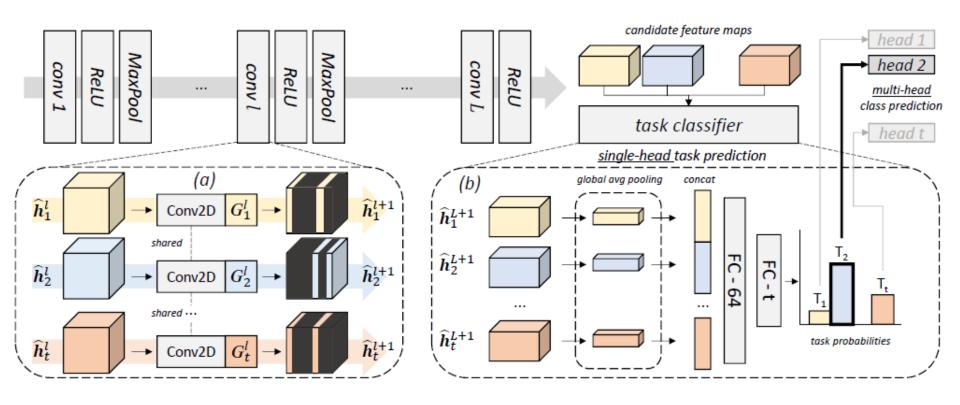
■ Conditional Channel Gate



Conditional Channel Gated Networks



■ Task Classifier





Conditional Convolution

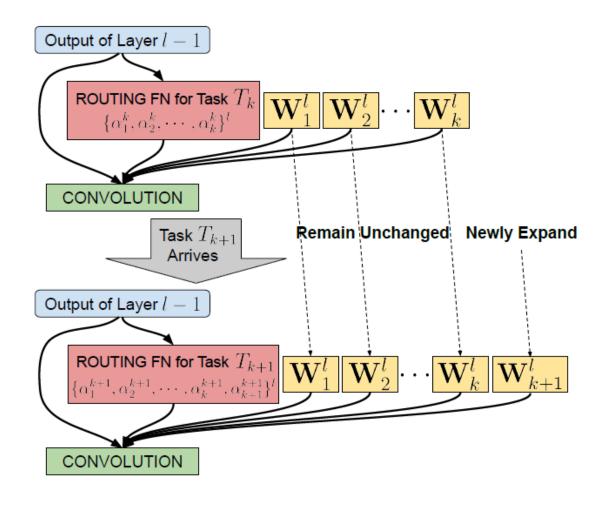
CondConv_n(
$$\mathbf{x}$$
) = $\sigma((\alpha_1 \mathbf{W}_1 + \alpha_2 \mathbf{W}_2 + \dots + \alpha_n \mathbf{W}_n) * \mathbf{x})$,
 $\alpha_i = \text{Sigmoid}(\text{GlobalAveragePool}(\mathbf{x})\mathbf{R}_i + \mathbf{b}_i)$,

$$M_{k+1}(\mathbf{x}) = C_{k+1}(\mathcal{B}(\mathbf{x}; \mathcal{W}_{1:(k+1)}, \mathcal{A}_{k+1})),$$

$$\underset{\mathcal{W}_{k+1},\mathcal{A}_{k+1},C_{k+1}}{\operatorname{arg\,min}} \sum_{(\mathbf{x},\mathbf{y})\in\mathcal{D}_{k+1}} l_{k+1}(M_{k+1}(\mathbf{x}),\mathbf{y})$$



■ Conditional Convolution



Optimal Relevance Mapping



■ What have they done?

$$\mathbb{M}_{\mathbb{P}k} \approx \prod_{k} \mathcal{L}_{R} \mathcal{N}(\mu_{\underline{k}}, \sigma_{\underline{k}}^{2})$$

$$\mathcal{L}_{R}(x_{k}; \beta) = \frac{1}{1 + \exp(-(\beta(x_{k} - 0.5))}$$



■ What did they claim?

Our proposed approach builds on the following Optimal Overlap Hypothesis: For a strictly continually trained deep neural network, catastrophic forgetting and remembering can be minimized, without additional memory or data, by learning optimal representational overlap, such that the representational overlap is reduced for unrelated tasks and increased for tasks that are similar.

Optimal Relevance Mapping



- What have they said?
 - Understanding Catastrophic Forgetting

Task
$$\frac{\operatorname{Loss}}{\log \mathcal{P}(\theta_{1}|D_{1}) = \log \mathcal{P}(D_{1}|\theta_{1}) + \log \mathcal{P}(\theta_{1}) - \log \mathcal{P}(D_{1}).}$$
Prior info
$$\log \mathcal{P}(\theta_{1:2}|D_{1:2}) = \log \mathcal{P}(D_{2}|\theta_{2}) + \log \mathcal{P}(\theta_{1}|D_{1})$$
Prior info
$$-\log \mathcal{P}(D_{2})$$
$$= \log \mathcal{P}(D_{2}|\theta_{2}) + \log \mathcal{P}(D_{1}|\theta_{1})$$
$$+ \log \mathcal{P}(\theta_{1}) - \log \mathcal{P}(D_{1}) - \log \mathcal{P}(D_{2}).$$

How is it proved?

$$\mathcal{P}(\theta_1, \mathbb{M}_{\mathbb{P}_1} | D_1) \propto \mathcal{P}(D_1 | \theta_{\mathbb{M}_{\mathbb{P}_1}}) \mathcal{P}(\theta_{\mathbb{M}_{\mathbb{P}_1}})$$

$$\mathcal{P}(\theta_{1:2}, \mathbb{M}_{\mathbb{P}_2} | D_{1:2}) \propto \mathcal{P}(D_2 | \theta_{\mathbb{M}_{\mathbb{P}_2}}) \mathcal{P}(\theta_1, \mathbb{M}_{\mathbb{P}_1} | D_1)$$

$$\propto \mathcal{P}(D_2 | \theta_{\mathbb{M}_{\mathbb{P}_2}}) \mathcal{P}(\theta_2'')$$

Optimal Relevance Mapping



Supervised Continual Learning

Algorithm 1 *RMN* Supervised Continual Learning

- 1: **Input:** data x, ground truth y for n tasks, prune parameter μ , corresponding task labels i paired with all x
- Given: parameters W & initilaized relevance mappings M_ℙ
- 3: **for** each task *i* **do**
- 4: $f(x_i; \mathbf{W}, \mathbb{M}_{\mathbf{P_i}}) \Rightarrow \hat{y_i} = \sigma((W \odot \mathbb{M}_{P_i}) \odot x_i)$
- 5: Compute Loss : $L(\hat{y_i}, y_i)$
- 6: Optional: Add Sparsity Loss: $L(\hat{y_i}, y_i) + (\mathbb{M}_{P_i})_{l_0}$
- 7: Backpropagate and optimize
- 8: Prune $\mathbb{M}_{\mathbb{P}} \leq \mu$ only.
- 9: Stabilize (fix) parameters in f where $\mathbb{M}_{\mathbb{P}} = 1$
- 10: **end for**
- 11: **Inference:** For data x and ground-truth task label i:
- 12: Output: f(x, i; W)

Optimal Relevance Algorithm 2 RMN Unsupervised Continual Learning

- 1: **Input:** data x, ground truth y, prune parameter μ
- 2: **Given:** parameters **W**, $\mathbb{M}_{\mathbb{P}est_{-}j}$ with $est_{-}j = 0$, Task Switch Detection Method TSD

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■ Unsupervised

- 3: **for** each task j **do**
- 4: Filter input x on $f(x; \mathbf{W}, \mathbb{M}_{\mathbb{P}_{0}, \mathbf{i} = 1})$
- $f(x; \mathbf{W}, \mathbb{M}_{\mathbb{P}_{\mathbf{est}_{-i}}}) \Rightarrow \hat{y}$ 5:
- Compute Loss : $L(\hat{y}, y)$ a Relevance modified Welsh's
- if TSD(x) is True then **t-test** on the KL divergence
- $est_{-}i + +$ 8:
- Add $\mathbb{M}_{\mathbb{P}est_{-i}}$ to learn-able parameter list
- $f(x; \mathbf{W}, \mathbb{M}_{\mathbb{P}_{\mathbf{est}_{-i}}}) \Rightarrow \hat{y}$ 10:
- Re-Compute Loss : $L(\hat{y}, y)$ 11:
- end if 12:
- 13: Backpropagate and optimize
- Sample x_q from standard Gaussian distribution with 14: same shape as x
- $f(x_g; \mathbf{W}, \mathbb{M}_{\mathbb{P}_{\mathbf{est}_{-i}}}) \Rightarrow \hat{y}$ 15:
- Compute Loss: $||\hat{y} 0||_2^2$ 16:
- Backpropagate and optimize 17:
- Prune $\mathbb{M}_{\mathbb{P}} \leq \mu$ only. 18:
- Stabilize (fix) parameters in f where $\mathbb{M}_{\mathbb{P}} \approx 1$ 19:
- 20: **end for**
- 21: **Inference:** For data x:
- 22: Output: $max_k f(x, k; W)$



■ Is that real?

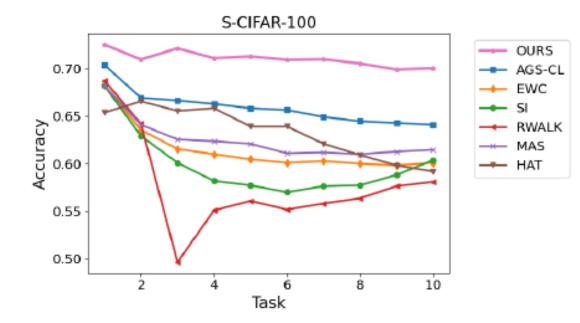


Figure 1. Average accuracy results on CIFAR-100 (10 tasks)

Summary and Discussion



■ Based on X (fc layer or t-test)

■ Fix previous params? $\sqrt{}$

■ Joint optimization? ×

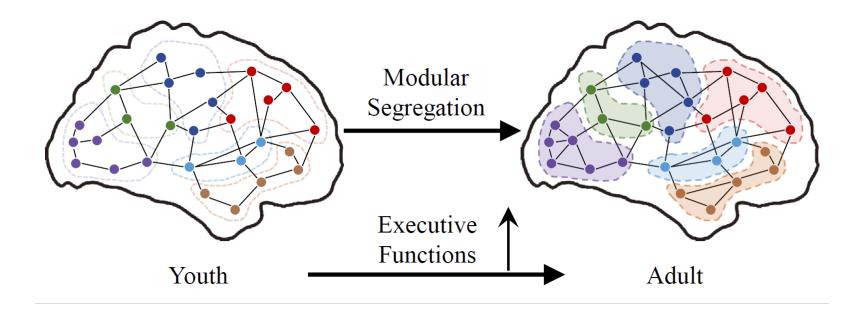


Our proposals



■ Motivation

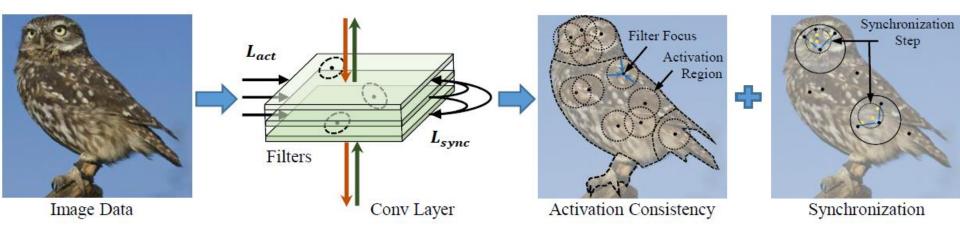
- Interpretation via Synchronization as Localization
- A Feature Map as an Entity -> Sync as Modules





■ Idea

- Minimize Entropy from several levels
- Sync (unsupervised) for Module Segmentation





Functional Module Level

SynC in clustering

$$rac{d heta_i}{dt} = \omega_i + rac{S}{N} \sum_{j=1}^N \sin(heta_j - heta_i), (i=1,\dots,N)$$

$$Nb_{\epsilon}(x) = \{ y \in \mathcal{D} | dist(y, x) \leq \epsilon \}$$

$$x_i(t+1) = x_i(t) + \frac{1}{|Nb_{\epsilon}(x(t))|} \cdot \sum_{y \in Nb_{\epsilon}(x(t))} \sin(y_i(t) - x_i(t))$$

SynC in mini-batch

$$L_{sync} = rac{1}{N} \sum_{x_i} rac{1}{|\,Nb_\epsilon(x_i)\,|} \sum_{x_i \in Nb_\epsilon(x_i)} dist(x_i,x_j)$$



Sync in mini-batch

$$L_{sync} = rac{1}{N} \sum_{x_i} rac{1}{|\,Nb_\epsilon(x_i)\,|} \sum_{x_i \in Nb_\epsilon(x_i)} dist(x_i,x_j)$$

Understanding

$$\begin{aligned} & L_{sync} = \frac{1}{N} \sum_{x_i} \frac{1}{|Nb_{\epsilon}(x_i)|} \sum_{x_j \in Nb_{\epsilon}(x_i)} dist(x_i, x_j) \\ & Word_{Embedding!} & \cong -\sum_{i,j} p(i)p(j|i) \log q(j|i) = H(j|i) \\ & p(i) = \frac{1}{N} \qquad \qquad q(j|i) = \frac{e^{-dist(x_i, x_j)/\tau_2}}{\sum_{j} e^{-dist(x_i, x_j)/\tau_2}} \\ & p(j|i) = \frac{Nb_{\epsilon}(x_i, x_j)}{\sum_{i} Nb_{\epsilon}(x_i, x_j)} = \left\{ \begin{array}{c} \frac{1}{|Nb_{\epsilon}(x_i)|}, & dist(x_i, x_j) < \epsilon \\ 0, & otherwise \end{array} \right. \end{aligned}$$



■ Motivation

- Functional modules on the whole structure
- Unsupervised knowledge embedding
- Knowledge embedding management

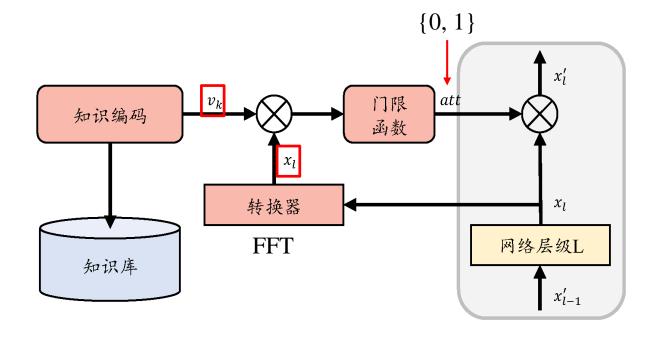
■ Idea

- Fourier Transform
- Sync to regular representation space
- Attention mechanism



■ Attention Structure

- Knowledge embedding as Key vector
- Hard attention -> activate the knowledge or not





- What's the cons?
 - 'Soft'-mask
 - No absolutely fixed parameter
 - Joint optimization

- So, Sync could be a promising way to it?
 - Stable functional module



■ What's the pros?

- **1. Constant memory.** To avoid unbounded systems, the consumed memory should be constant w.r.t. the number of tasks or length of the data stream.
- **6. Problem agnostic** continual learning is not limited to a specific setting (e.g. only classification).
- **7. Adaptive** systems learn from available unlabeled data as well, opening doors for adaptation to specific user data.
- **8. No test time oracle** providing the task label should be required for prediction.
- **9. Task revisiting** of previously seen tasks should enable enhancement of the corresponding task knowledge.
- **10. Graceful forgetting.** Given an unbounded system and infinite stream of data, selective forgetting of trivial information is an important mechanism to achieve balance between stability and plasticity.



- What's the pros?
 - Local, Disentangled, Interpretable, Comparable
 - Knowledge management for Continual learning
 - Multi-source, partial, model-based Transfer learning
 - Zero-shot via compositional generalization
 - Match with existing knowledge systems
 - Interact with human beings
 - •

Proposal		Oxford 102 Flowers						
		Method	Task 1	Task 2	Task 3	Task 4	Avg.	数据挖掘实验室
		Finetuning	10.0 (-20.3)	5.1 (-17.1)	6.7 (-13.6)	17.3 (0.0)	9.8	Data Mining Lab
		Freezing	30.3 (0.0)	39.8 (0.0)	32.0 (0.0)	33.1 (0.0)	33.8	
		Joint	54.6 (+24.3)	58.9 (+11.5)	57.7 (+4.5)	47.0 (0.0)	54.6	
		EWC [14]	12.1 (-18.2)	11.6 (-38.1)	9.3 (-24.4)	25.8 (0.0)	14.7	
■ Plan		HAT [41]	17.2 (-12.7)	19.3 (-28.5)	28.6 (+1.4)	31.6 (0.0)	24.2	
		PackNet [26]	32.0 (0.0)	53.7 (0.0)	43.6 (0.0)	37.9 (0.0)	41.8	
		TFM w/o FN	36.4 (0.0)	54.1 (0.0)	38.6 (0.0)	39.0 (0.0)	42.0	
•	Exan	TFM	36.4 (0.0)	53.8 (0.0)	45.5 (0.0)	37.6 (0.0)	43.3	
		CUBS 200 Birds						
•	Adar	Method	Task 1	Task 2	Task 3	Task 4	Avg.	
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•	Expe	Joint	48.7 (+11.1)	52.1 (+6.0)	50.7 (+1.5)	51.9 (0.0)	50.8	
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•	Cana	PackNet [26]	35.3 (0.0)	42.8 (0.0)	44.4 (0.0)	45.9 (0.0)	42.1	~
	Gene	TFM w/o FN	42.9 (0.0)	44.1 (0.0)	48.3 (0.0)	49.1 (0.0)	46.1	g,
	comp	TFM	42.9 (0.0)	43.1 (0.0)	49.9 (0.0)	48.8 (0.0)	46.2	e, etc.)
	Com	Stanford 40 Actions						, (10.)
		Method	Task 1	Task 2	Task 3	Task 4	Avg.	
•	Thec	Finetuning	24.4 (-10.5)	26.5 (-7.7)	17.6 (-16.8)	28.9 (0.0)	24.4	tional)
		Freezing	34.9 (0.0)	29.4 (0.0)	30.1 (0.0)	30.5 (0.0)	31.2	
		Joint	45.7 (+10.8)	40.3 (+4.8)	43.2 (-1.1)	40.2 (0.0)	42.4	
•	Perfo	EWC [14]	24.2 (-10.7)	28.2 (-2.0)	25.2 (-5.6)	34.3 (0.0)	28.0	
		HAT [41]	25.7 (-1.0)	25.5 (-2.7)	30.1 (-2.1)	34.4 (0.0)	28.9	
		PackNet [26]	32.5 (0.0)	32.9 (0.0)	36.7 (0.0)	34.3 (0.0)	34.1	
		TFM w/o FN	35.3 (0.0)	38.3 (0.0)	39.2 (0.0)	38.0 (0.0)	37.7	
		TFM	35.3 (0.0)	37.2 (0.0)	42.0 (0.0)	37.2 (0.0)	38.0	



■ Plan

- Exam existing CL methods in the same setting
- Adapt from FcaNet, add HAT and Sync
- Experiments of CL and Interpretability(?)
- General Applications (transfer/zero-shot learning, compact existing networks & efficient networks, etc.)
- Theoretical guarantee of accuracy boundary (optional)
- Perform as a conference paper

Thank you



